

Generative Adversarial Network

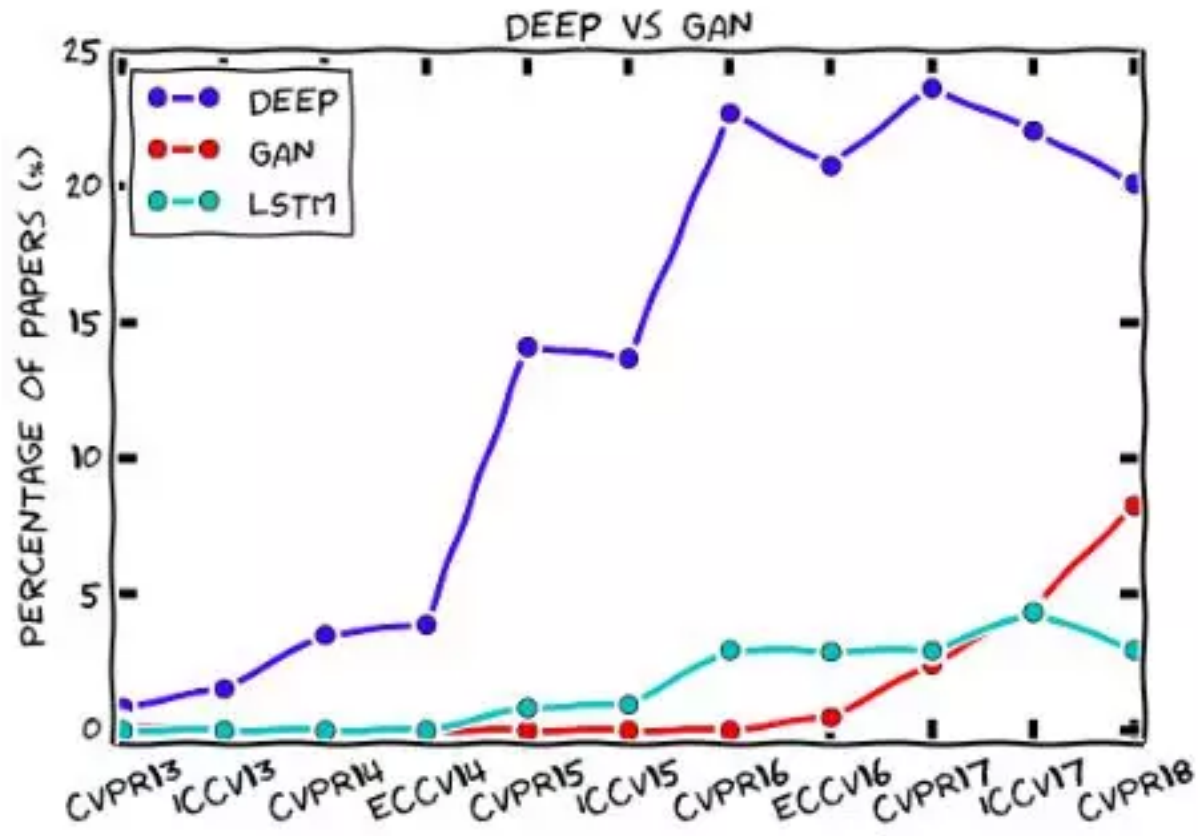
Liangjie

Outline

- Basic theory (GAN, DCGAN)
- Recent improvement (WGAN, AAE, WAE)
- Applications (CGAN, Text2Img, DeblurGAN)

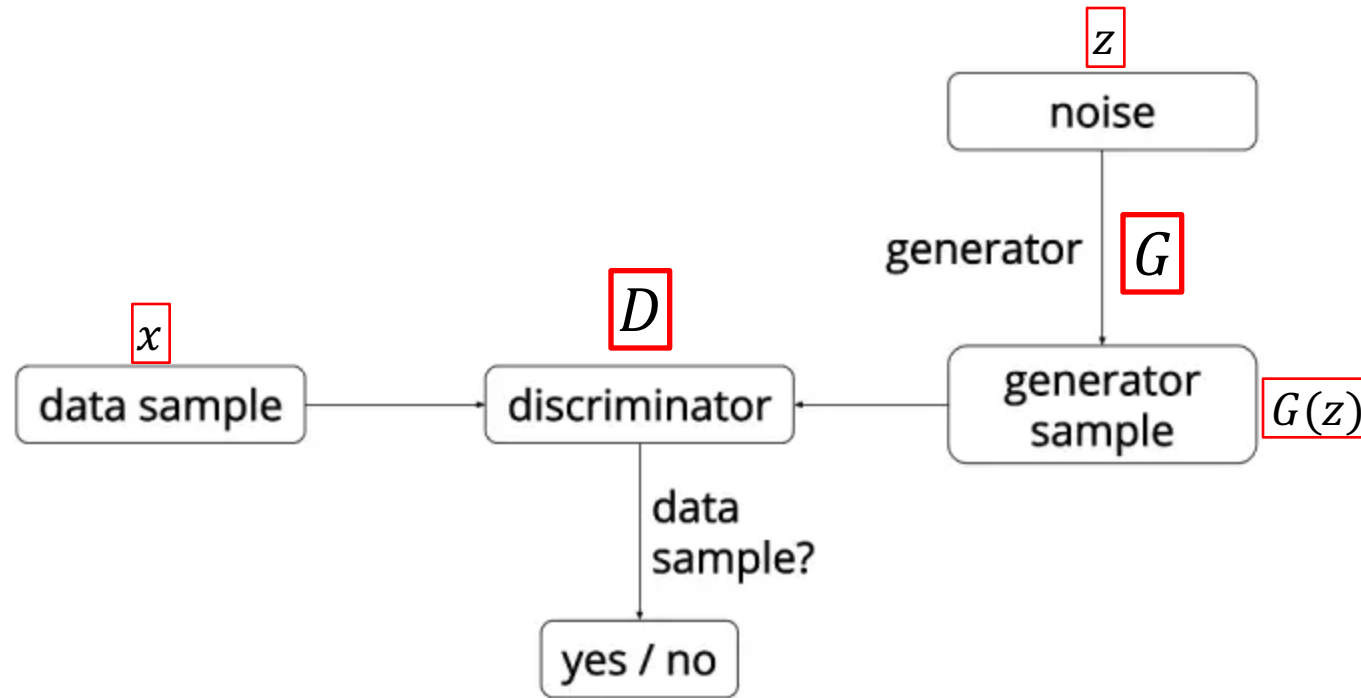
A hot topic

GAN related papers per community in CVPR 2018:



- style transfer/cycle GAN/domain adaption: **13**
 - Photo enhancement/deblur/high-resolution reconstruction/...: **7**
 - Optimizing GAN theory: **6**
 - Image synthesis: **10**
 - human face related: **7**
 - human pose related: **4**
 - Person Re-ID: **3**
 - Others ...
- **TOTAL**: 75+, around 8% of 979 papers.

The idea of GAN



Competition in this game drives both teams (**G** and **D**) to improve their capacity until the counterfeits are indistinguishable from the genuine articles.

The Algorithm

$$\min_G \max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(1 - D(G(\mathbf{z})))] .$$

The probability that \mathbf{x} is a real sample.

Algorithm 1 Minibatch stochastic gradient descent training of generative adversarial nets. The number of steps to apply to the discriminator, k , is a hyperparameter. We used $k = 1$, the least expensive option, in our experiments.

for number of training iterations **do**

for k steps **do**

- Sample minibatch of m noise samples $\{\mathbf{z}^{(1)}, \dots, \mathbf{z}^{(m)}\}$ from noise prior $p_g(\mathbf{z})$.
- Sample minibatch of m examples $\{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(m)}\}$ from data generating distribution $p_{\text{data}}(\mathbf{x})$.
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m [\log D(\mathbf{x}^{(i)}) + \log(1 - D(G(\mathbf{z}^{(i)})))] .$$

end for

- Sample minibatch of m noise samples $\{\mathbf{z}^{(1)}, \dots, \mathbf{z}^{(m)}\}$ from noise prior $p_g(\mathbf{z})$.
- Update the generator by descending its stochastic gradient:

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(1 - D(G(\mathbf{z}^{(i)}))) .$$

end for

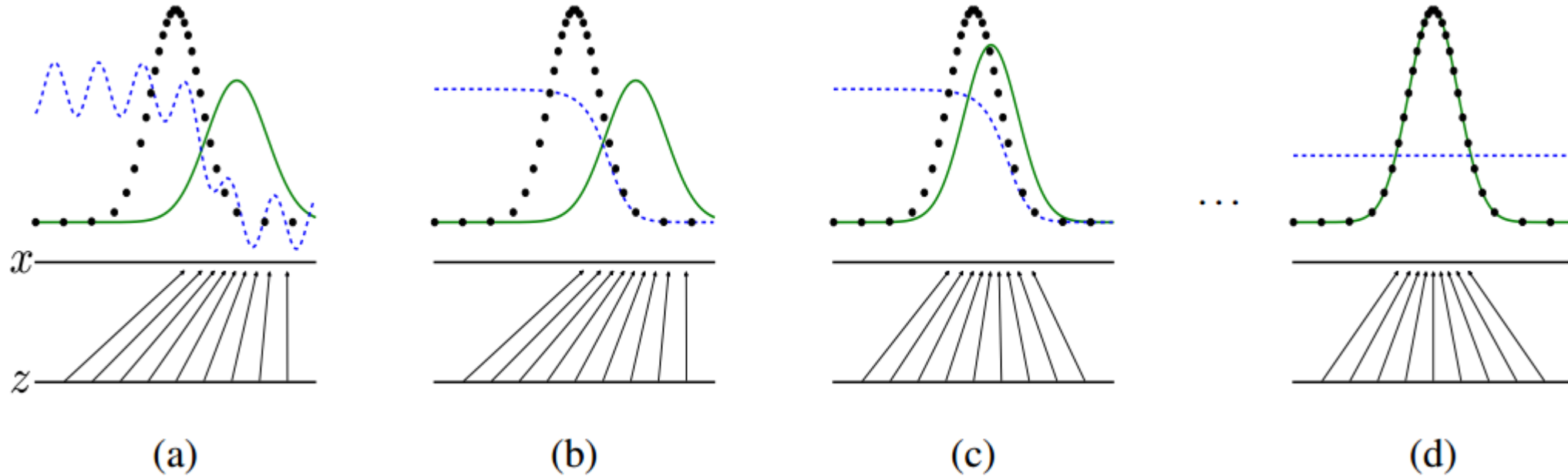
The gradient-based updates can use any standard gradient-based learning rule. We used momentum in our experiments.



First train **D** for several times,
Then train **G**.

k is hard to control!

The training process of the original GAN



The original state.
Both G and D are
not powerful.

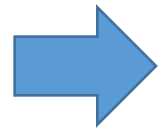
After training D.
D can tell which
sample is real.

After training G.
G can generate
'real' samples.

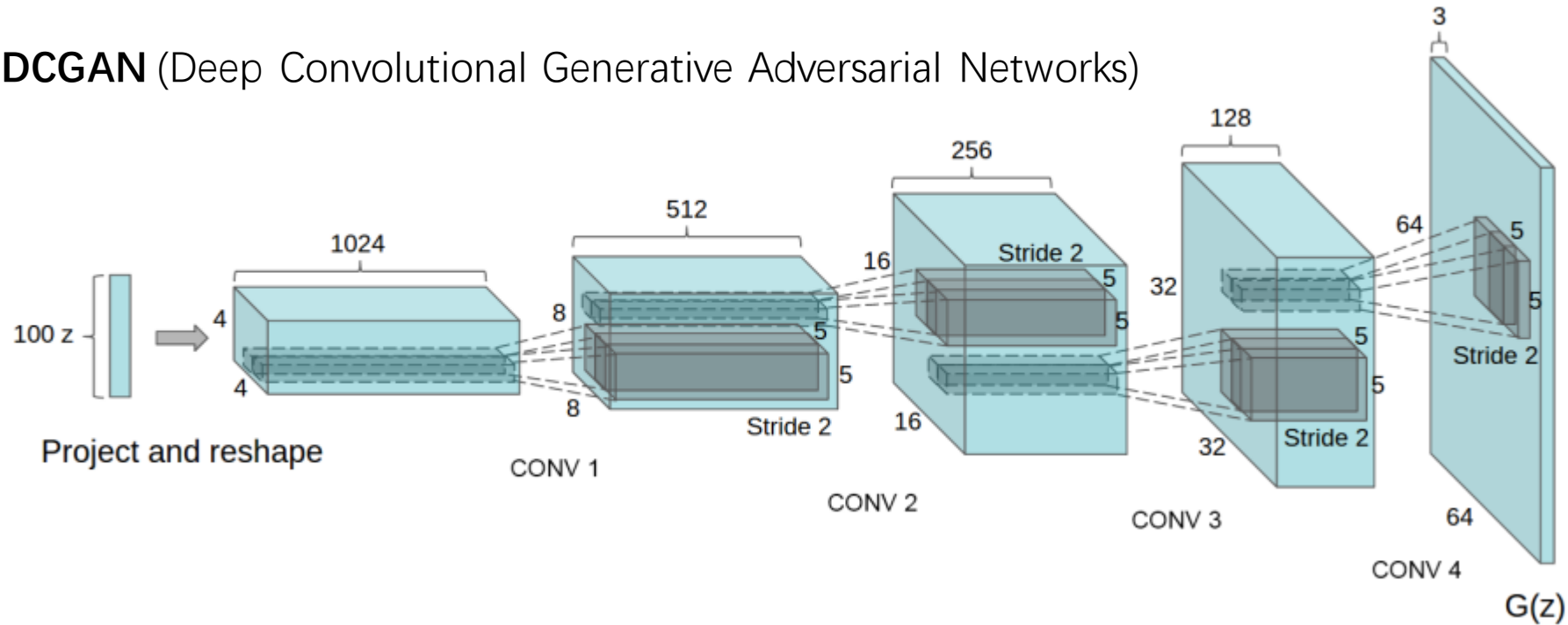
The final state.
Both G and D
are powerful.

The weakness

- 1) The structure is too simple thus lacks ability.
- 2) The generative model and the discriminative model should utilize the deep convolutional network.

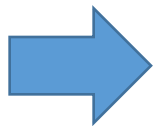


DCGAN (Deep Convolutional Generative Adversarial Networks)



Still have weakness

1. The training process is unstable.
2. Hardly to control the ability of the **G** and **D**.
3. The gradient always disappears.
4. Do not have an index to show the performance of the model.
5. The obtained samples lack of diversity.



WGAN (Wasserstein GAN)

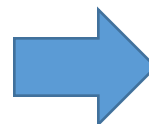
WGAN (Wasserstein GAN)

Algorithm 1 WGAN, our proposed algorithm. All experiments in the paper used the default values $\alpha = 0.00005$, $c = 0.01$, $m = 64$, $n_{\text{critic}} = 5$.

Require: : α , the learning rate. c , the clipping parameter. m , the batch size.
 n_{critic} , the number of iterations of the critic per generator iteration.

Require: : w_0 , initial critic parameters. θ_0 , initial generator's parameters.

```
1: while  $\theta$  has not converged do
2:   for  $t = 0, \dots, n_{\text{critic}}$  do
3:     Sample  $\{x^{(i)}\}_{i=1}^m \sim \mathbb{P}_r$  a batch from the real data.
4:     Sample  $\{z^{(i)}\}_{i=1}^m \sim p(z)$  a batch of prior samples.
5:      $g_w \leftarrow \nabla_w \left[ \frac{1}{m} \sum_{i=1}^m f_w(x^{(i)}) - \frac{1}{m} \sum_{i=1}^m f_w(g_\theta(z^{(i)})) \right]$ 
6:      $w \leftarrow w + \alpha \cdot \text{RMSProp}(w, g_w)$ 
7:      $w \leftarrow \text{clip}(w, -c, c)$ 
8:   end for
9:   Sample  $\{z^{(i)}\}_{i=1}^m \sim p(z)$  a batch of prior samples.
10:   $g_\theta \leftarrow -\nabla_\theta \frac{1}{m} \sum_{i=1}^m f_w(g_\theta(z^{(i)}))$ 
11:   $\theta \leftarrow \theta - \alpha \cdot \text{RMSProp}(\theta, g_\theta)$ 
12: end while
```



The modifications:

1. No sigmoid in last layer of **D**.
2. No $\log(a)$ in the loss of the **G** and **D**.
3. For **D**, clip the updated parameter to $[-c, c]$.

The problem in GAN

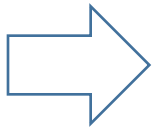
1. If the **D** has strong ability to make decision, the gradient of **G** will disappear

When training the **D**: we maximize the equation:

$$\begin{aligned} L(D, g_\theta) &= \mathbb{E}_{x \sim P_r} \log D(x) + \mathbb{E}_{x \sim P_g} \log[1 - D(x)] \\ &= P_r(x) \log D(x) + P_g(x) \log[1 - D(x)] \end{aligned}$$

The derivative of $D(x)$ equals 0:

$$\frac{P_r(x)}{D(x)} - \frac{P_g(x)}{1 - D(x)} = 0.$$



The optimal discriminator :

$$D^*(x) = \frac{P_r(x)}{P_r(x) + P_g(x)}$$

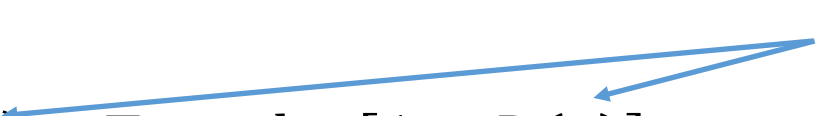
The problem in GAN

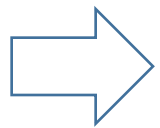
1. If the **D** has strong ability to make decision, the gradient of **G** will disappear

When training the **G**: we minimize the equation:

$$\mathbb{E}_{x \sim P_r} \log D(x) + \mathbb{E}_{x \sim P_g} \log[1 - D(x)]$$

$D^*(x) = \frac{P_r(x)}{P_r(x) + P_g(x)}$





$$\mathbb{E}_{x \sim P_r} \log \frac{P_r(x)}{\frac{1}{2}(P_r(x) + P_g(x))} + \mathbb{E}_{x \sim P_g} \log \left[1 - \frac{P_r(x)}{\frac{1}{2}(P_r(x) + P_g(x))} \right] - 2 \log 2$$

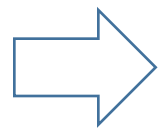
The problem in GAN

1. If the **D** has strong ability to make decision, the gradient of **G** will disappear

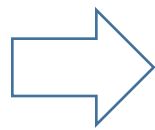
KL divergence : $KL(P_1 || P_2) = \mathbb{E}_{x \sim P_r} \log \frac{P_1}{P_2}$

JS divergence : $JS(P_1 || P_2) = \frac{1}{2} KL(P_1 || (P_1 + P_2)/2) + \frac{1}{2} KL(P_2 || (P_1 + P_2)/2)$

$$\mathbb{E}_{x \sim P_r} \log \frac{P_r(x)}{\frac{1}{2}(P_r(x) + P_g(x))} + \mathbb{E}_{x \sim P_g} \log \left[1 - \frac{P_r(x)}{\frac{1}{2}(P_r(x) + P_g(x))} \right] - 2 \log 2$$



$$= 2JS(P_r || P_g) - 2 \log 2$$



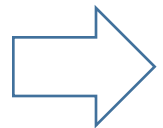
When training the **G**, we minimize the JS divergence between real distribution and generative distribution.

The problem in GAN

1. If the **D** has strong ability to make decision, the gradient of **G** will disappear

$$JS(P_r || P_g) = \begin{cases} \log 2 & P_r = 0, P_g \neq 0; \text{ or } P_r \neq 0, P_g = 0 \\ 0 & P_r = 0, P_g = 0; \text{ or } P_r \neq 0, P_g \neq 0 \end{cases}$$

The two distribution can hardly have combinations since z is obtained randomly and the intrinsic dimension is much lower than the real space.



The gradient of **G** disappears.

The problem in GAN

2. The training process is unstable.

For **G**, it minimizes the object function:

$$\begin{aligned}\mathbb{E}_{x \sim P_g} [-\log D^*(x)] &= KL(P_r || P_g) - \mathbb{E}_{x \sim P_g} \log[1 - D^*(x)] \\ &= KL(P_r || P_g) - 2JS(P_r || P_g) + 2\log 2 + \mathbb{E}_{x \sim P_r} \log D^*(x)\end{aligned}$$

$$\Rightarrow KL(P_r || P_g) - 2JS(P_r || P_g)$$

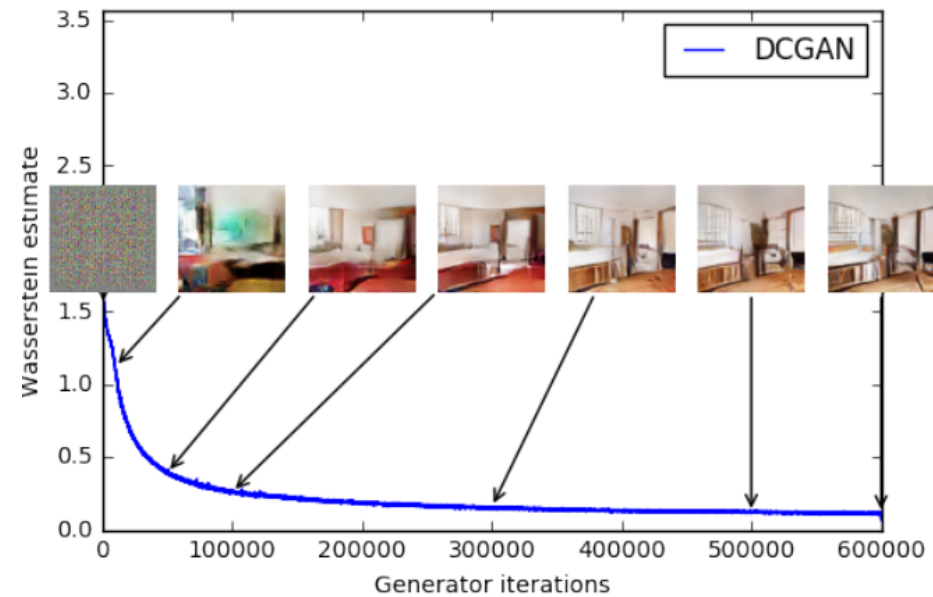
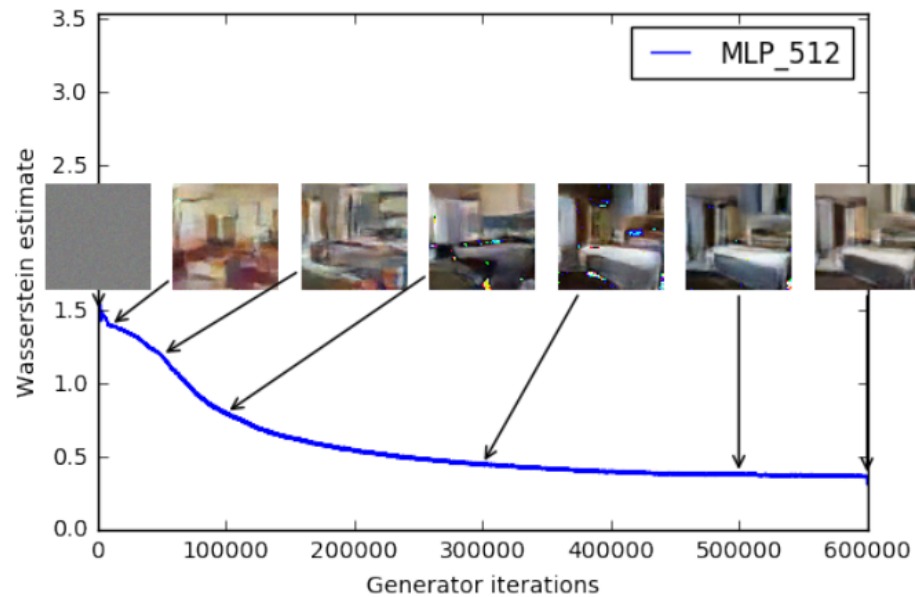
One to close while another to far! \Rightarrow unstable

The problem in GAN

3. Lack an index to show the performance of the model

Wasserstein Distance (Earth-Mover distance):

$$W(P_r, P_g) = \inf_{\gamma \sim \Pi(P_r, P_g)} \mathbb{E}_{(x, y) \sim \gamma} [\|x - y\|]$$



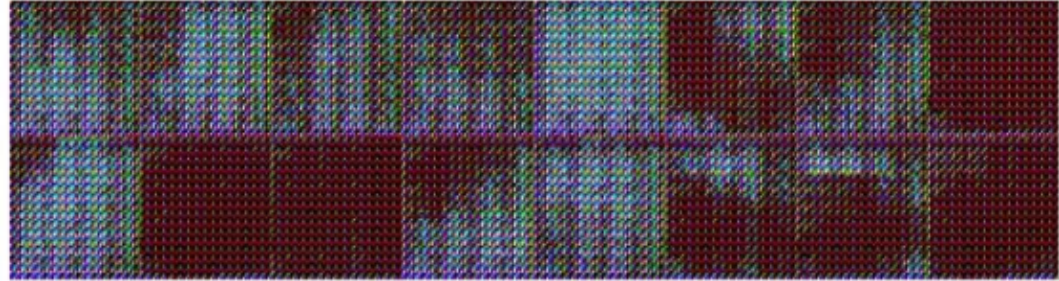
Wasserstein GAN

Advantages:

- does not need to carefully control the capacity of G and D
- alleviates the mode collapse problem
- provides a metric of model capacity during training
- does not require well-designed network architectures

Some Results

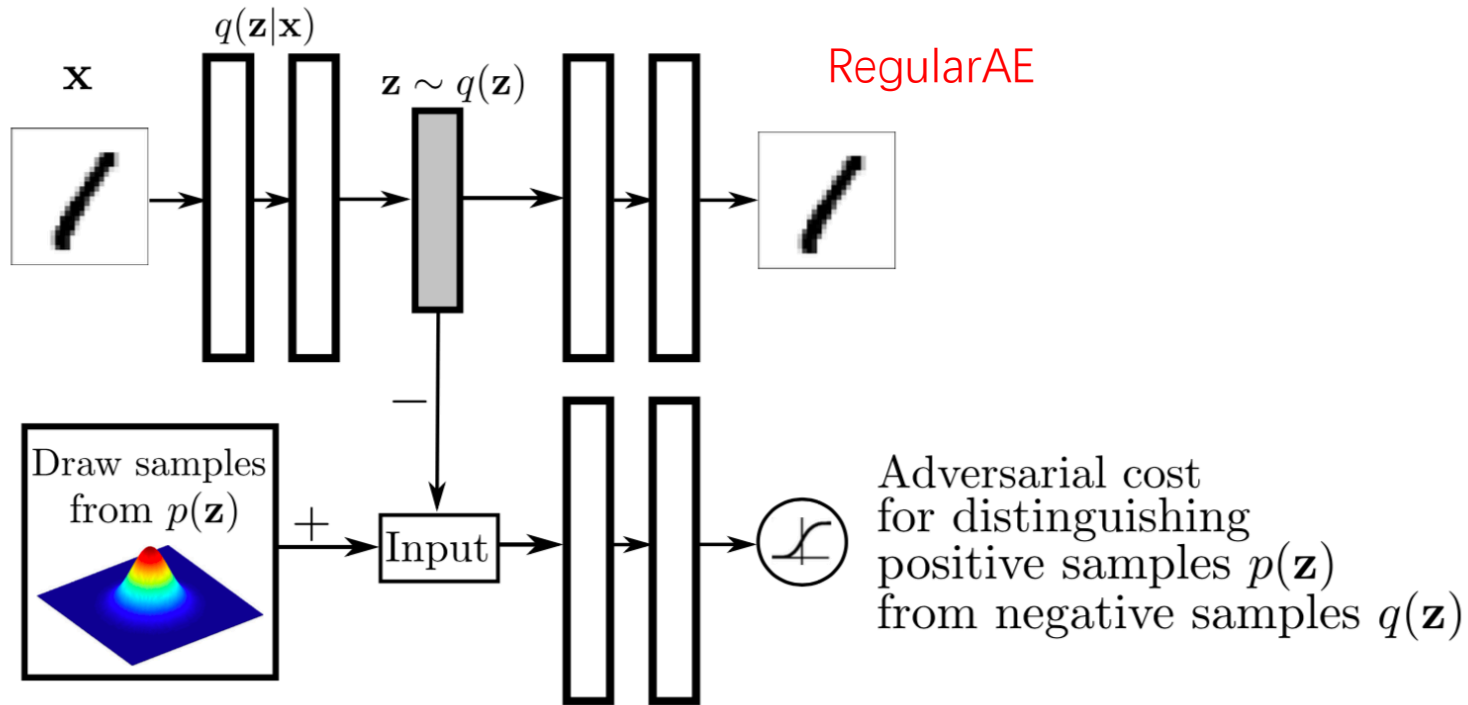
WGANs vs DCGANs (without BN)



WGANs vs GANs (without CNN)

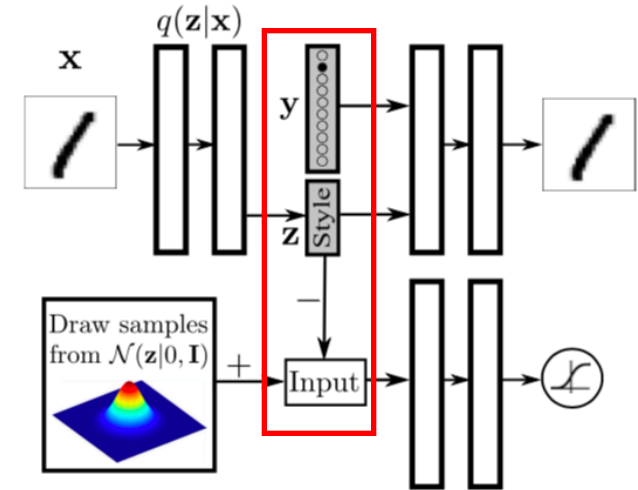
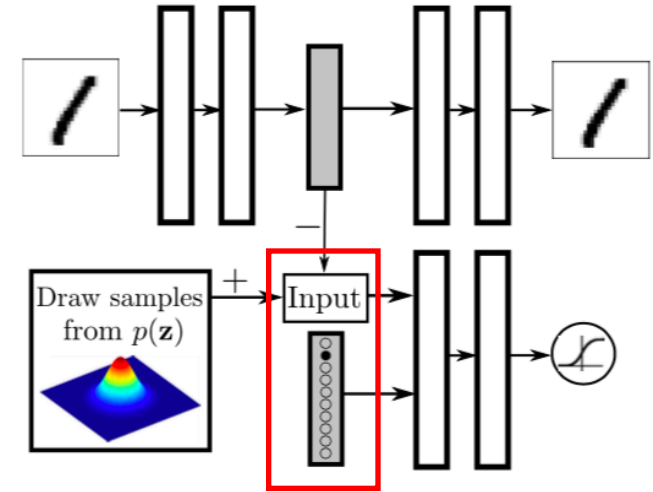


Adversarial Auto-Encoders



$D : z$ is derived from the encoder of the random sampled from prior distribution

Finally: q_z has same distribution with p_z , we can feed the random sampled latent code to the decoder, to generate new samples.



Adversarial Auto-Encoders



(a) MNIST



(b) SVHN

Wasserstein Auto-Encoders

- Encoder:**
- Based on a specified divergence, **matches** the encoded distribution Q_Z of training samples to the prior P_Z .
 - Ensures that the latent codes fed to the decoders are **informative to reconstruct** the training sample.

- Decoder:**
- According to the cost function, **reconstruct** the encoded training sample.

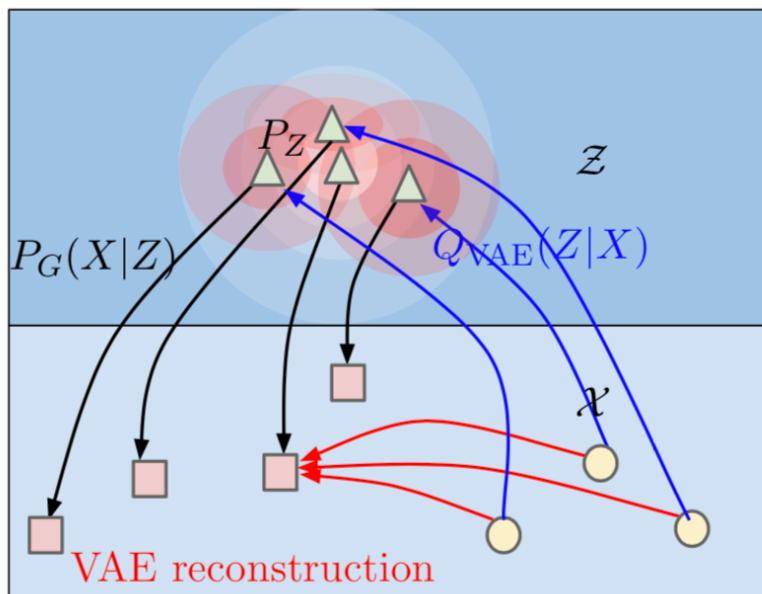
Loss Function: Optimal transport cost $W_c(P_X, P_G)$, a family of Wasserstein distance

$$D_{\text{WAE}}(P_X, P_G) := \inf_{Q(Z|X) \in \mathcal{Q}} \mathbb{E}_{P_X} \mathbb{E}_{Q(Z|X)} [\boxed{c(X, G(Z))}] + \lambda \cdot \boxed{\mathcal{D}_Z(Q_Z, P_Z)},$$

Reconstruction loss Penalty

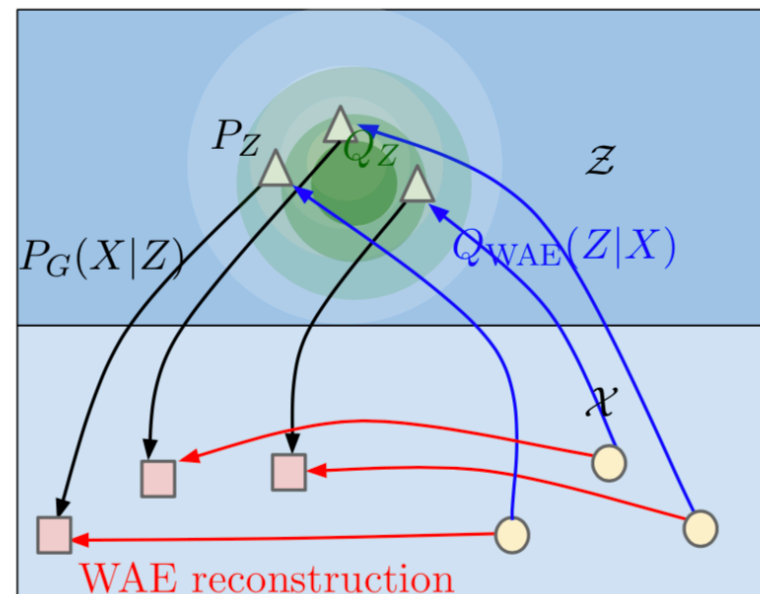
Wasserstein Auto-Encoders

(a) VAE



For each samples in X (yellow circle), forces $Q(Z|X)$ (triangle) to match $P(Z)$ (white shape).

(b) WAE



Forces $Q_Z = \int Q(Z|X)dP_X$ to match $P(Z)$ (green ball).

Wasserstein Auto-Encoders

Algorithm 1 Wasserstein Auto-Encoder with GAN-based penalty (WAE-GAN).

Require: Regularization coefficient $\lambda > 0$.

Initialize the parameters of the encoder Q_ϕ , decoder G_θ , and latent discriminator D_γ .

while (ϕ, θ) not converged **do**

 Sample $\{x_1, \dots, x_n\}$ from the training set

 Sample $\{z_1, \dots, z_n\}$ from the prior P_Z

 Sample \tilde{z}_i from $Q_\phi(Z|x_i)$ for $i = 1, \dots, n$

 Update D_γ by ascending:

$$\frac{\lambda}{n} \sum_{i=1}^n \log D_\gamma(z_i) + \log(1 - D_\gamma(\tilde{z}_i))$$

 Update Q_ϕ and G_θ by descending:

$$\frac{1}{n} \sum_{i=1}^n c(x_i, G_\theta(\tilde{z}_i)) - \lambda \cdot \log D_\gamma(\tilde{z}_i)$$

end while

Algorithm 2 Wasserstein Auto-Encoder with MMD-based penalty (WAE-MMD).

Require: Regularization coefficient $\lambda > 0$, characteristic positive-definite kernel k .

Initialize the parameters of the encoder Q_ϕ , decoder G_θ , and latent discriminator D_γ .

while (ϕ, θ) not converged **do**

 Sample $\{x_1, \dots, x_n\}$ from the training set

 Sample $\{z_1, \dots, z_n\}$ from the prior P_Z

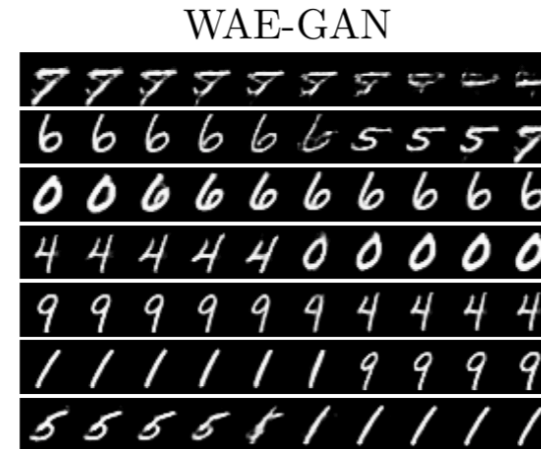
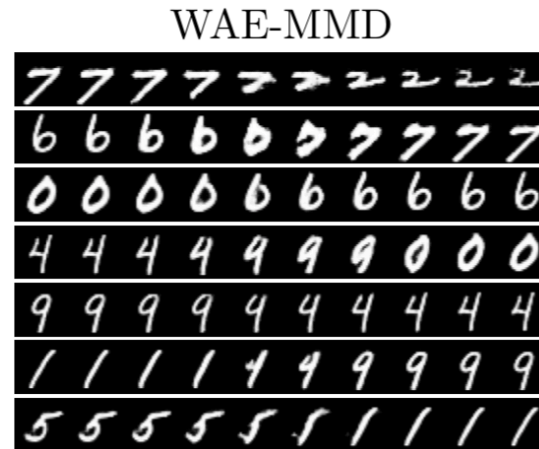
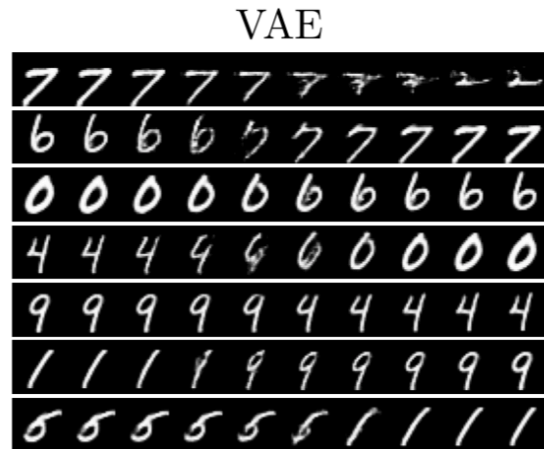
 Sample \tilde{z}_i from $Q_\phi(Z|x_i)$ for $i = 1, \dots, n$

 Update Q_ϕ and G_θ by descending:

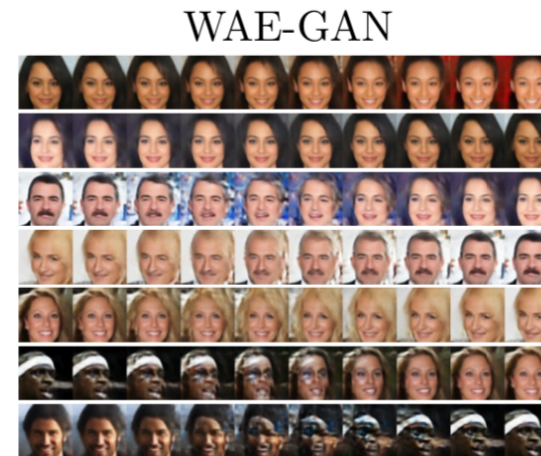
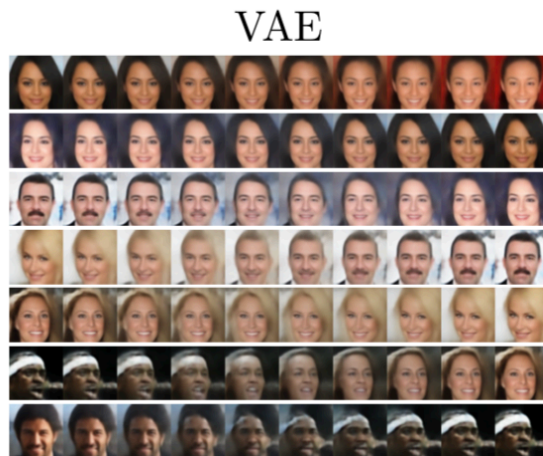
$$\begin{aligned} & \frac{1}{n} \sum_{i=1}^n c(x_i, G_\theta(\tilde{z}_i)) + \frac{\lambda}{n(n-1)} \sum_{\ell \neq j} k(z_\ell, z_j) \\ & + \frac{\lambda}{n(n-1)} \sum_{\ell \neq j} k(\tilde{z}_\ell, \tilde{z}_j) - \frac{2\lambda}{n^2} \sum_{\ell, j} k(z_\ell, \tilde{z}_j) \end{aligned}$$

end while

Wasserstein Auto-Encoders



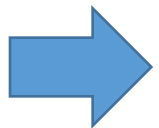
MNIST:
28*28



celebA:
64*64

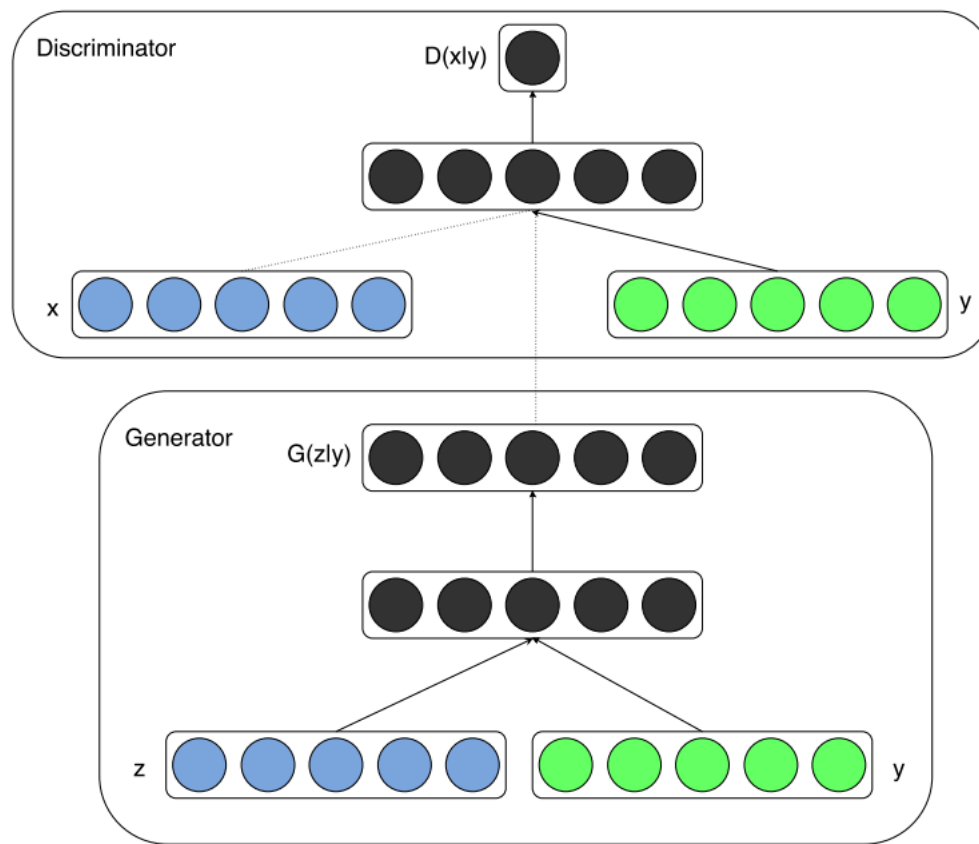
Applications

1. Generate new samples for training, especially those hard to collect.
 2. Combine with various low-level vision tasks such as segmentation, etc.
 3. Complete the broken image (inpainting).
 4. Generate high resolution image from lower one.
 5. Generate images from the text descriptions.
- ...



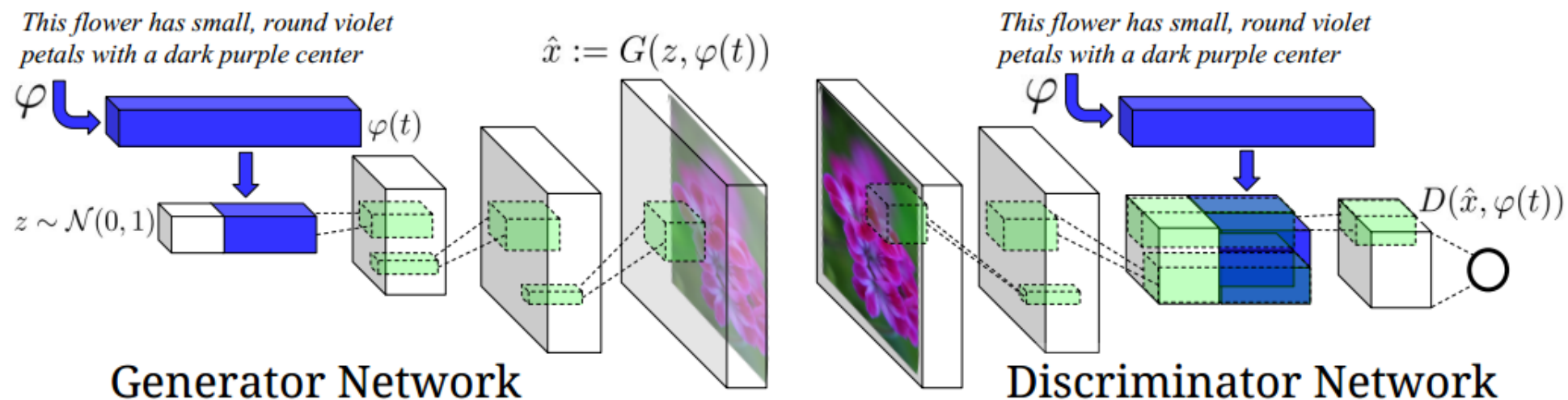
GAN can be combined with any task that generates some new things, e.g., the mask in segmentation task, the broken part in image inpainting task, or the high-resolution image, etc.

Conditional GAN

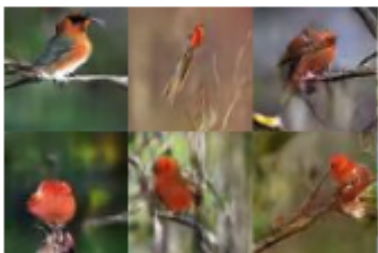


$$\min_G \max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x}|\mathbf{y})] + \mathbb{E}_{\mathbf{z} \sim p_z(\mathbf{z})} [\log(1 - D(G(\mathbf{z}|\mathbf{y})))].$$

Text2Img



this small bird has a pink breast and crown, and black primaries and secondaries.



this magnificent fellow is almost all black with a red crest, and white cheek patch.



the flower has petals that are bright pinkish purple with white stigma



this white and yellow flower have thin white petals and a round yellow stamen



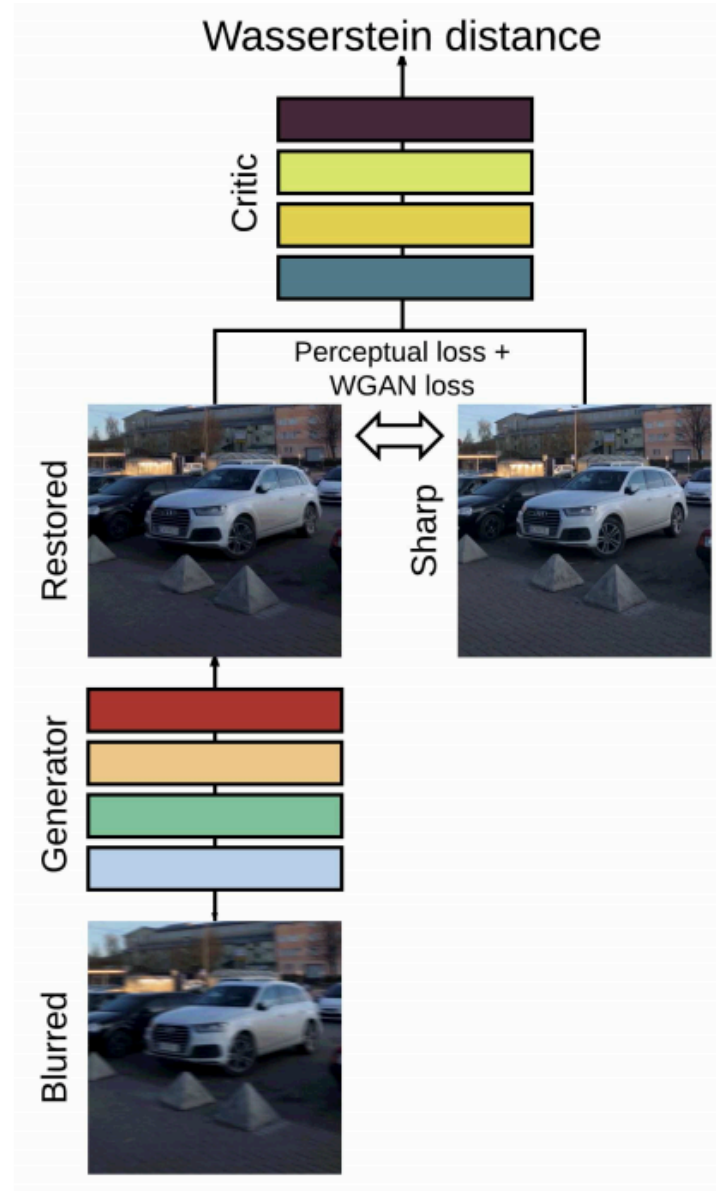
DeblurGAN

WGAN loss:

Wasserstein distance

Perceptual loss:

the **difference** between the VGG-19 conv3.3 feature maps of the sharp and restored images.



Thanks